

MCAP EOC Tutorials for Maryland are designed specifically for the Maryland College and Career Ready Standards to prepare students for the Maryland Comprehensive Assessment Program (MCAP). EOC Categories are at the heart of MCAP EOC Tutorial structure – bringing category-based learning to the student experience, and category-based performance and progress tracking to the teacher experience.

Math Tutorials offer targeted instruction, practice and review designed to develop computational fluency, deepen conceptual understanding, and apply mathematical practices. They automatically identify and address learning gaps down to elementary-level content, using adaptive remediation to bring students to grade-level no matter where they start. Students engage with the content in an interactive, feedback-rich environment as they progress through standards-aligned modules. By constantly honing the ability to apply their knowledge in abstract and real world scenarios, students build the depth of knowledge and higher order skills required to demonstrate their mastery when put to the test.

In each module, the Learn It and Try It make complex ideas accessible to students through focused content, modeled logic and process, multi-modal representations, and personalized feedback as students reason through increasingly challenging problems. The Review It offers a high impact summary of key concepts and relates those concepts to students' lives. The Test It assesses students' mastery of the module's concepts, providing granular performance data to students and teachers after each attempt. To help students focus on the content most relevant to them, unit-level pretests and posttests can quickly identify where students are strong and where they're still learning.

Test-Taking Strategies for EOC Tutorials allow students to practice and apply learning approaches that will hone their testtaking skills and focus them for success on the day of their EOC test.

1. POINTS, LINES, AND FIGURES

• POINTS, RAYS, LINE SEGMENTS, LINES, AND FIGURES

- **G.CO.A.1** Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc.
- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.

PARALLEL AND PERPENDICULAR LINES

- G.GPE.B.5 Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems.
- G.R.3 Determine cases where a given proposition is true or false.
- G.R.4 Identify an unstated assumption that makes a problem well-posed or makes a particular method viable.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
- **G.CO.C.9** Prove and/or apply theorems about lines and angles. Theorems include: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent; points on a perpendicular bisector of a line segment are exactly those equidistant from the segment's endpoints.
- **G.CO.A.1** Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc.

2. LINES AND ANGLES

PARALLEL LINES AND ANGLE RELATIONSHIPS

- **C.M.6** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, requiring application of course-level knowledge and skills articulated in the standards.
- **G.CO.C.9** Prove and/or apply theorems about lines and angles. Theorems include: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent; points on a perpendicular bisector of a line segment are exactly those equidistant from the segment's endpoints.
- **G.R.3** Determine cases where a given proposition is true or false.

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- G.R.4 Identify an unstated assumption that makes a problem well-posed or makes a particular method viable.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.

PERPENDICULAR BISECT OR AND ANGLE BISECT OR THEOREMS

- **G.R.3** Determine cases where a given proposition is true or false.
- **G.R.4** Identify an unstated assumption that makes a problem well-posed or makes a particular method viable.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
- **G.CO.C.10** Prove and/or apply theorems about triangles. Theorems include: measures of interior angles of a triangle sum to 180°; base angles of isosceles triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point.
- **G.CO.D.12** Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometric software, etc.). Copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment; and constructing a line parallel to a given line through a point not on the line.

3. TRIANGLES

• TRIANGLE ANGLE THEOREMS

- **G.M.6** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, requiring application of course-level knowledge and skills articulated in the standards.
- **G.CO.C.10** Prove and/or apply theorems about triangles. Theorems include: measures of interior angles of a triangle sum to 180°; base angles of isosceles triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point.
- G.R.3 Determine cases where a given proposition is true or false.
- G.R.4 Identify an unstated assumption that makes a problem well-posed or makes a particular method viable.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
- **G.R.8** Use a combination of algebraic and geometric reasoning to justify or refute propositions or conjectures about geometric figures.

• TRIANGLE BISECTORS

- **G.CO.D.12** Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometric software, etc.). Copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment; and constructing a line parallel to a given line through a point not on the line.
- **G.M.6** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, requiring application of course-level knowledge and skills articulated in the standards.
- **G.CO.C.10** Prove and/or apply theorems about triangles. Theorems include: measures of interior angles of a triangle sum to 180°; base angles of isosceles triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point.
- G.R.2 Identify a correct method and justification given two or more chains of reasoning.
- G.R.3 Determine cases where a given proposition is true or false.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.

4. PARALLELOGRAMS AND RECTANGLES

PARALLELOGRAMS AND RECTANGLES

- G.R.2 Identify a correct method and justification given two or more chains of reasoning.
- G.R.3 Determine cases where a given proposition is true or false.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
- **G.CO.C.11** Prove theorems about parallelograms. Theorems include: opposite sides are congruent, opposite angles are congruent, the diagonals of a parallelogram bisect each other, and conversely, rectangles are parallelograms with congruent diagonals.
- **G.M.6** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, requiring application of course-level knowledge and skills articulated in the standards.

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5. SQUARES AND RHOMBI

• SQUARES AND RHOMBI

- G.R.2 Identify a correct method and justification given two or more chains of reasoning.
- G.R.3 Determine cases where a given proposition is true or false.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
- **G.CO.C.11** Prove theorems about parallelograms. Theorems include: opposite sides are congruent, opposite angles are congruent, the diagonals of a parallelogram bisect each other, and conversely, rectangles are parallelograms with congruent diagonals.
- **G.M.6** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, requiring application of course-level knowledge and skills articulated in the standards.

6. GEOMETRIC TRANSFORMATIONS

• TRANSFORMATIONS ON THE COORDINATE PLANE

- G.R.2 Identify a correct method and justification given two or more chains of reasoning.
- G.R.3 Determine cases where a given proposition is true or false.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- **G.SRT.A.2** Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides.
- **G.CO.A.5** Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another.
- **G.CO.B.6** Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.
- **G.SRT.A.1a** A dilation takes a line not passing through the center of the dilation to a parallel line, and leaves a line passing through the center unchanged.

• DILATIONS, TRANSLATIONS, ROTATIONS, AND REFLECTIONS

- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- **G.CO.A.5** Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another.
- **G.CO.B.6** Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.
- **G.SRT.A.2** Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides.
- G.R.3 Determine cases where a given proposition is true or false.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.

7. INTRODUCTION TO CONGRUENCE

• TRIANGLES AND CONGRUENCE TRANSFORMATIONS

- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- **G.CO.B.6** Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.
- **G.CO.B.7** Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent.

CONGRUENCE OF OT HER POLYGONS

- G.M.6 Solve multi-step contextual word problems with degree of difficulty appropriate to the course, requiring application of course-level knowledge and skills articulated in the standards.
- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- G.CO.B.6 Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on

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a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.

- **G.R.3** Determine cases where a given proposition is true or false.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
- **G.CO.A.3** Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself.

8. INTRODUCTION TO SIMILARITY

- TRIANGLES AND SIMILARITY TRANSFORMATIONS
 - G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
 - G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
 - **G.SRT.A.2** Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides.
 - **G.SRT.B.5** Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures.
 - **G.SRT.B.4** Prove theorems about triangles. Theorems include: a line parallel to one side of a triangle divides the other two proportionally, and conversely; the Pythagorean Theorem proved using triangle similarity.

• SIMILARITY OF OT HER POLYGONS

- **G.M.6** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, requiring application of course-level knowledge and skills articulated in the standards.
- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- **G.SRT.A.2** Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides.

9. TRIANGLES AND TRIGONOMETRY

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- **G.M.6-2** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, requiring application of course-level knowledge and skills articulated in involving right triangles in an applied setting.
- G.SRT.C.8 Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.
- **G.SRT.B.4** Prove theorems about triangles. Theorems include: a line parallel to one side of a triangle divides the other two proportionally, and conversely; the Pythagorean Theorem proved using triangle similarity.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
- **G.R.3** Determine cases where a given proposition is true or false.

• TRIGONOMETRIC RATIOS

- G.SRT.C.8 Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.
- G.SRT.C.7 Explain and use the relationship between the sine and cosine of complementary angles.
- **G.R.8** Use a combination of algebraic and geometric reasoning to justify or refute propositions or conjectures about geometric figures.
- **G.M.6-2** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, requiring application of course-level knowledge and skills articulated in involving right triangles in an applied setting.

10. CIRCLE BASICS AND ANGLES 1

• CIRCLE BASICS

• **G.C.A.2** Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle.

• SECANTS, ANGLES, AND INTERCEPTED ARCS

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• G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.

11. CIRCLE BASICS AND ANGLES 2

• CENT RAL ANGLES, INSCRIBED ANGLES, AND CHORDS

- **G.R.5** Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
- **G.C.A.2** Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle.

• TANGENTS, ANGLES, AND INTERCEPTED ARCS

- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
- G.C.A.2 Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle.

12. AREA AND STANDARD EQUATION OF CIRCLES

AREA OF CIRCLES AND SECTORS

- **G.M.6-1** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, involving perimeter, area, or volume that require the use 8th grade algebra skills.
- **G.C.B.5** Derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector.
- G.R.3 Determine cases where a given proposition is true or false.
- G.R.4 Identify an unstated assumption that makes a problem well-posed or makes a particular method viable.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.
- G.R.8 Use a combination of algebraic and geometric reasoning to justify or refute propositions or conjectures about geometric figures.

• CIRCLES

- **G.GPE.A.1** Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation.
- **G.CO.A.1** Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc.

13. MEASUREMENT, CONGRUENCY, AND SIMILARITY OF CIRCLES

CIRCUMFERENCE AND ARC LENGTH

- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- **G.C.B.5** Derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector.

• CONGRUENT AND SIMILAR CIRCLES

• **G.CO.B.6** Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.

14. LINES IN THE COORDINATE PLANE

- SLOPE
 - G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
 - **G.GPE.B.5** Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems.

• SLOPE-INTERCEPT FORM OF A LINEAR EQUATION

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- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- G.GPE.B.5 Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems.

15. COORDINATE GEOMETRY

• LENGTH AND THE DISTANCE FORMULA

- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- G.GPE.B.6 Find the point on a directed line segment between two given points that partitions the segment in a given ratio.
- **G.GPE.B.7** Use coordinates to compute perimeters of polygons and areas of triangles and rectangles, e.g., using the distance formula.

• MIDPOINT FORMULA ON THE COORDINATE PLANE

- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- G.GPE.B.6 Find the point on a directed line segment between two given points that partitions the segment in a given ratio.

• CONJECT URES IN COORDINATE GEOMETRY

- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- G.GPE.B.4 Use coordinates to prove simple geometric theorems algebraically.

16. PERIMETER AND AREA

• PERIMETER ON THE COORDINATE PLANE

- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- **G.GPE.B.7** Use coordinates to compute perimeters of polygons and areas of triangles and rectangles, e.g., using the distance formula.
- **G.M.6-1** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, involving perimeter, area, or volume that require the use 8th grade algebra skills.
- G.GPE.B.4 Use coordinates to prove simple geometric theorems algebraically.

• AREA ON THE COORDINATE PLANE

- G.R.6 Apply geometric reasoning in a coordinate setting, and/or use coordinates to draw geometric conclusions.
- **G.M.6-1** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, involving perimeter, area, or volume that require the use 8th grade algebra skills.

17. CONSTRUCTIONS AND THREE-DIMENSIONAL FIGURES

- CONSTRUCTIONS
 - **G.CO.D.12** Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometric software, etc.). Copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment; and constructing a line parallel to a given line through a point not on the line.

RELATING TWO-DIMENSIONAL FIGURES TO THREE-DIMENSIONAL SOLIDS

• **G.GMD.B.4-1** Identify the shapes of two-dimensional cross-sections of three-dimensional objects, and identify threedimensional objects generated by rotations of two-dimensional objects.

18. PRISMS, PYRAMIDS, AND SPHERES

VOLUME OF PRISMS AND PYRAMIDS

- G.GMD.A.3 Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.
- **G.M.6-1** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, involving perimeter, area, or volume that require the use 8th grade algebra skills.

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SURFACE AREA AND VOLUME OF SPHERES

- **G.GMD.B.4-1** Identify the shapes of two-dimensional cross-sections of three-dimensional objects, and identify threedimensional objects generated by rotations of two-dimensional objects.
- **G.GMD.A.1** Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. Use dissection arguments, Cavalieri's principle, and informal limit arguments.
- G.GMD.A.3 Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.

19. CYLINDERS AND CONES

VOLUME OF CYLINDERS AND CONES

- **G.GMD.A.3** Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.
- **G.M.6-1** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, involving perimeter, area, or volume that require the use 8th grade algebra skills.
- G.R.2 Identify a correct method and justification given two or more chains of reasoning.

20. MODELING SITUATIONS

MODELING SITUATIONS WITH GEOMETRY

- **G.MG.A.2** Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).
- **G.M.5** Use and/or provide a reasonable estimate of a quantity needed to solve a problem.
- **G.MG.A.3** Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).

21. VOLUME OF SIMILAR AND COMPOSITE SHAPES

VOLUME OF SIMILAR SOLIDS

- G.GMD.A.3 Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.
- **C.M.6-1** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, involving perimeter, area, or volume that require the use 8th grade algebra skills.
- G.R.2 Identify a correct method and justification given two or more chains of reasoning.

• VOLUME OF COMPOSITE SOLIDS

- **G.M.6-1** Solve multi-step contextual word problems with degree of difficulty appropriate to the course, involving perimeter, area, or volume that require the use 8th grade algebra skills.
- G.GMD.A.3 Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.
- G.R.2 Identify a correct method and justification given two or more chains of reasoning.
- G.R.3 Determine cases where a given proposition is true or false.
- G.R.5 Construct, autonomously, chains of reasoning that will justify or refute geometric propositions or conjectures.

22. TEST-TAKING STRATEGIES

- STUDY HABITS
- BEING PREPARED AND GETTING STARTED
- WORDING IN TEST QUESTIONS
- WORDING IN ANSWER CHOICES
- QUESTIONS WITH PASSAGES AND VISUAL DATA
- ESSAY AND SHORT ANSWER QUESTIONS
- WORD PROBLEMS